

# Discussion: "Strike While the Iron Is Hot: Optimal Monetary Policy With a Nonlinear Phillips Curve"

by Peter Karadi, Anton Nakov, Galo Nuño, Ernesto Pastén, Dominik Thaler

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Timo Haber<sup>1</sup>

Inflation: Drives and Dynamics, October 25 2024, Cleveland, Ohio

<sup>1</sup>**De Nederlandsche Bank.**

*Disclaimer: Views expressed here are my own and do not necessarily reflect official positions of De Nederlandsche Bank or the Eurosystem*

**This Paper** analyzes optimal monetary policy in the context of a **nonlinear Phillips curve**.

- Model with state-dependent pricers, a central bank, and households that consume and supply labor.
- Golosov-Lucas Framework implies non-linear Phillips Curve whereas Calvo is linear. [not new]
- Inflation hurts because it increases the frequency of **menu costs** that need to be paid.
- Investigate fully **non-linear** optimal monetary policy in this setting.

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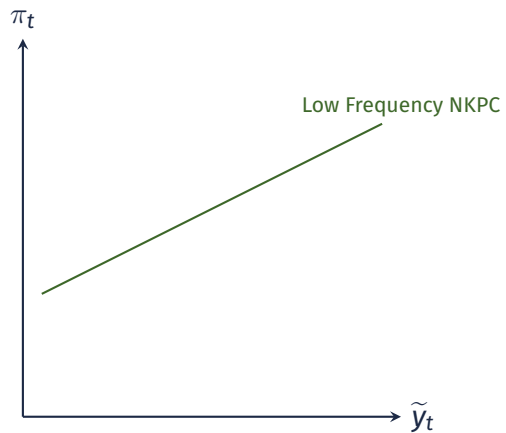
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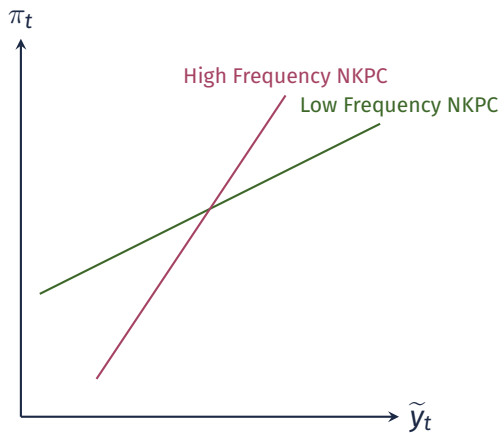
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## The paper in two graphs

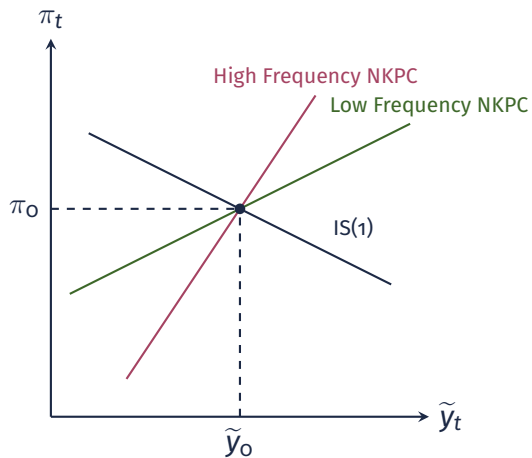


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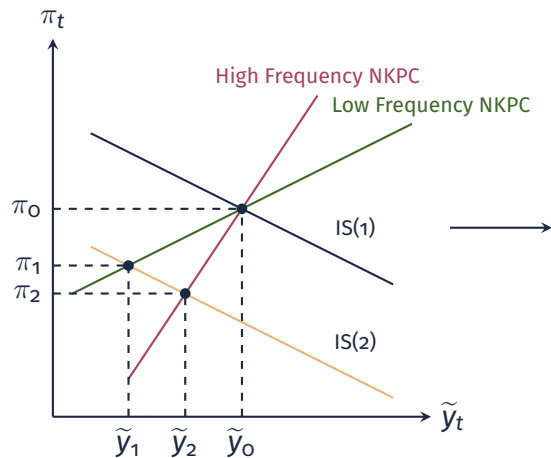




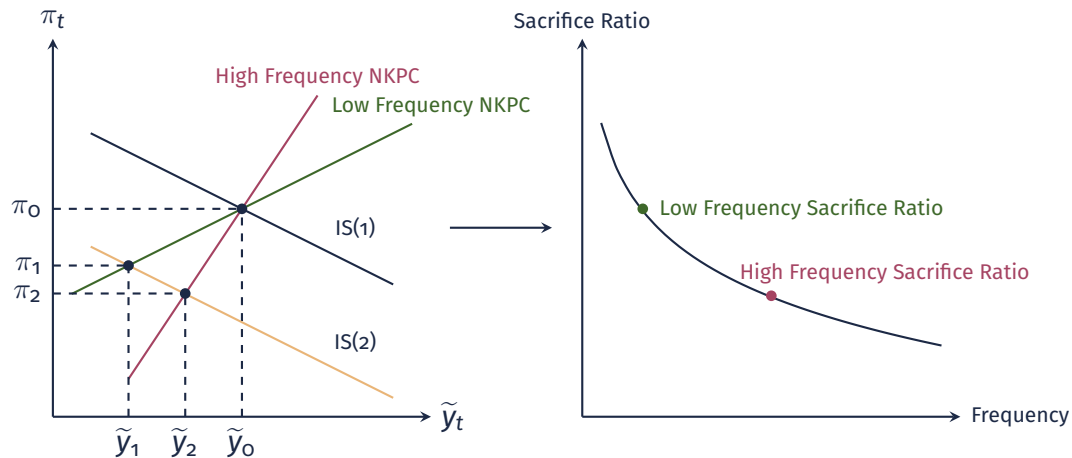
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## Main Message

**Strike while the iron is hot: aggressive inflation stabilization in case of large shocks.**

### More normative results:

1. Steady State Inflation rate is **positive** due to asymmetry in profit function.
2. Optimal response to TFP shocks retains **divine coincidence**.
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- Great and **highly relevant** paper. [▶ Post-Covid Inflation](#) [▶ Isabel Schnabel: Quote](#)
- **Intuitive** story with clear message. [▶ Main Graph](#)
- **Impressive** use of state of the art techniques that pushes the frontier. [see also Dávila and Schaab (2022), Le Grand et al (2022), Nuño and Thomas (2022) and others]

## Plan for the Discussion

- Comment **#1**: How relevant is the non-linearity?
- Comment **#2**: An aggregate estimate of the non-linear PC
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## Comment #1: How relevant is the non-linearity?

- **My view:** Paper can assess optimal policy with state-dependent prices **quantitatively**

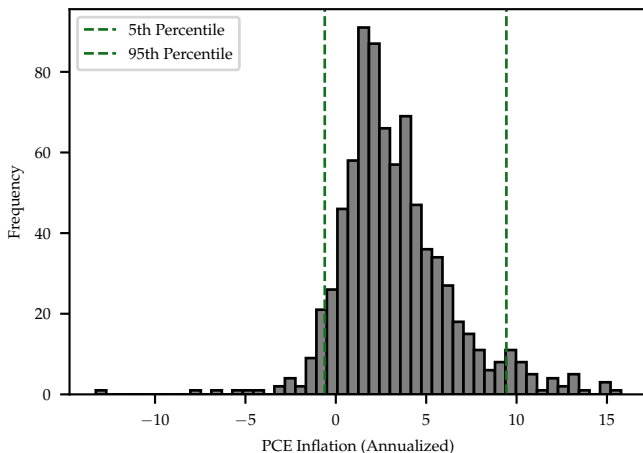
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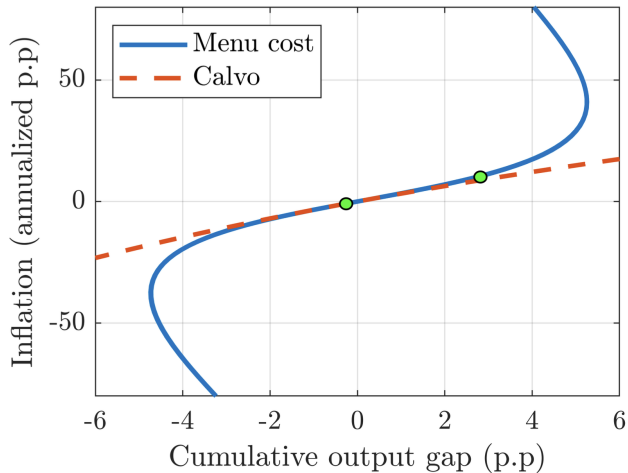
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Histogram of US inflation rates (1959-2024)

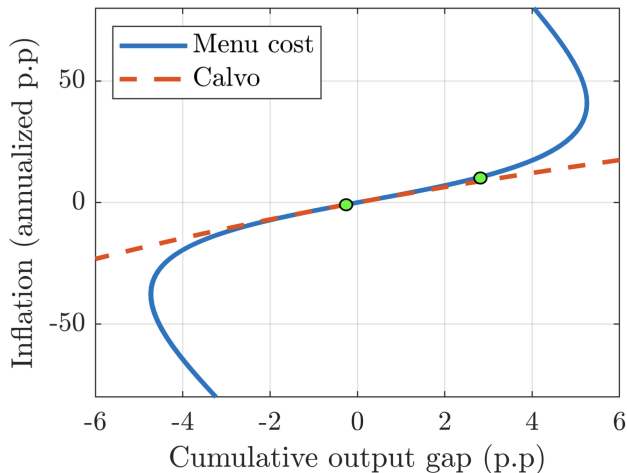


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- The non-linearity of the PC only starts biting for the 95th percentile of inflation realizations

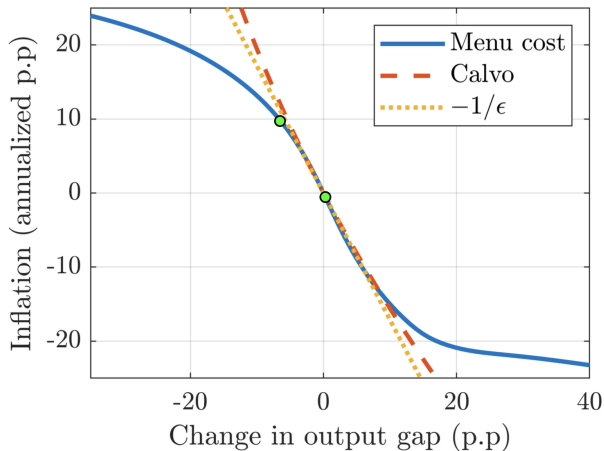
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**The same is true for the optimal targeting rule**

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### My suggestion:

- Can we obtain some estimate for the welfare loss following Calvo instead of the non-linear optimal rule **given historical inflation**?
- **Crude way**: Assume 5% of the time large cost push (ie. above 10%). Otherwise they are below. Compute weighted welfare loss.
- **More sophisticated**: Calculate welfare gap as function of inflation and integrate using historical inflation distribution?

### More broadly:

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## Comment #2: An empirical estimate of the non-linear PC

- Key to results is the **shape and magnitude** of the response of inflation and output to shocks [as they are related to the shape of the PC]
- Validate these objects by comparing them to **empirical** evidence [Ascari and Haber (2021)]
- We estimate **size-dependent** impulse responses to inflation and output following monetary policy shocks in the US between 1969 and 2007.

$$y_{t+h} = \alpha_h + \tau_h t + \beta_h e_t + \zeta_h(e_t \cdot |e_t|) + \sum_{k=1}^K \gamma_{h,k} w_{t,k} + v_{t+h}, \quad (1)$$

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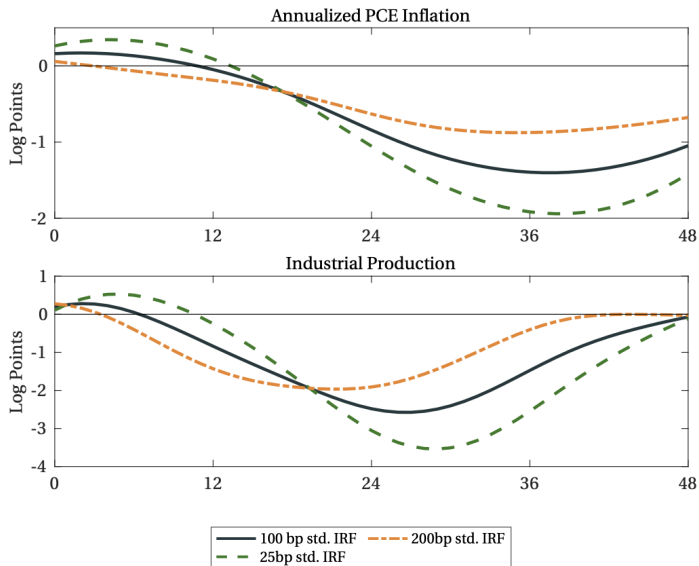
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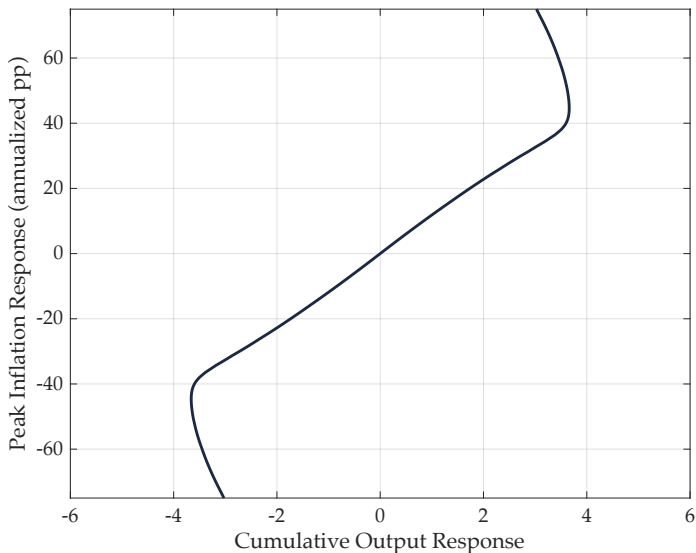
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Qualitatively the "same" non-linear responses as in the optimal case ▶ Model IRFs



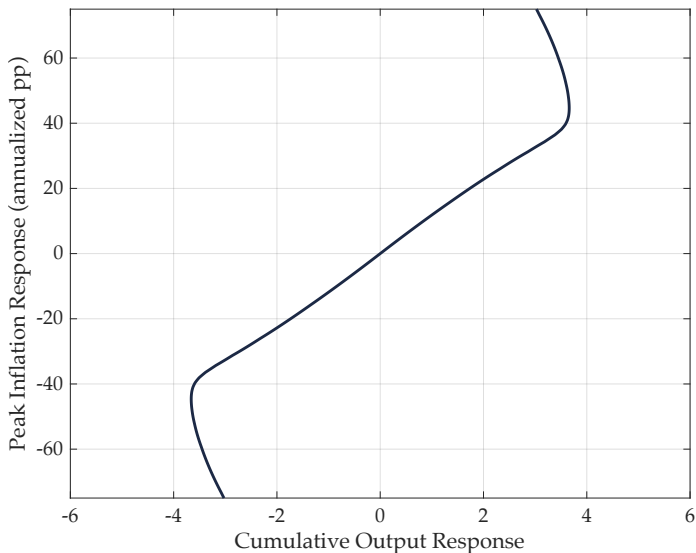
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Simulate IRFs for different shock sizes and **replicate** the non-linear PC ▶ Model NKPC
- **Qualitative:**  
Remarkably similar in shape
- **Quantitative:** Much steeper, with even higher values where non-linearity kicks in



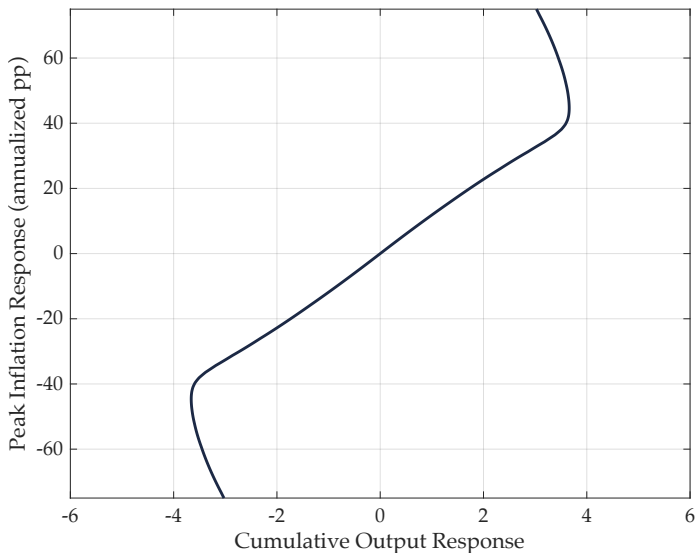
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### My suggestion:

- Currently the model is calibrated to match **frequency and size** of price changes in the US
- Can we go a step further and use direct **empirical** evidence on the non-linear Phillips curve? [Gagnon, 2009; Karadi and Reiff, 2019; Alvarez and Neumeyer, 2020; Alexandrov, 2020); Ascari and Haber (2021), Cavallo (2024) ]
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## Comment #3: Uncertainty and Imperfect Information

- The cost-push shock and policy response are modeled assuming **perfect foresight**.  
→ Policy maker knows the evolution of the sacrifice ratio at **every point**
- In **reality**: Sacrifice ratio is uncertain object & CB has imperfect information
- For example, Beaudry et al (2024) argue that post-2020 data was consistent with **flat PC**
- Raises potential for policy mistakes based on evolution of PC [Orphanides and Williams , 2007]

**Striking the Iron vs Treading carefully in a dark room?**

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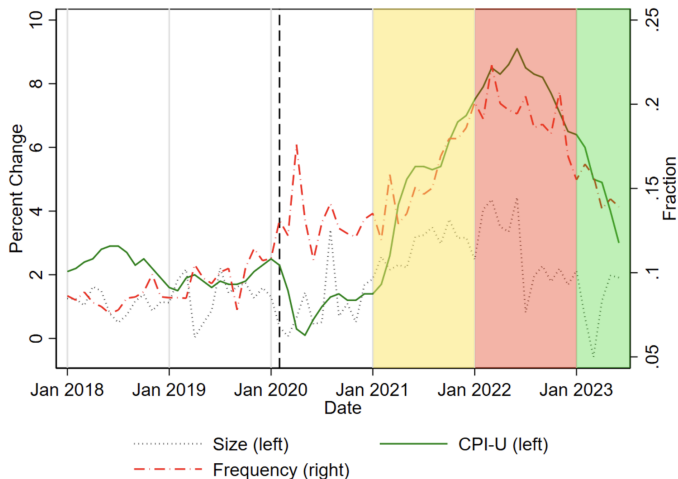
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## Comment #4: When shall we strike the iron?

- In the model the shock raises inflation **immediately** but in the recently inflation rises and falls more **gradually**
- Green marks the area where we do want to land smoothly
- Red marks the area where we should strike the iron
- But what about the yellow area?

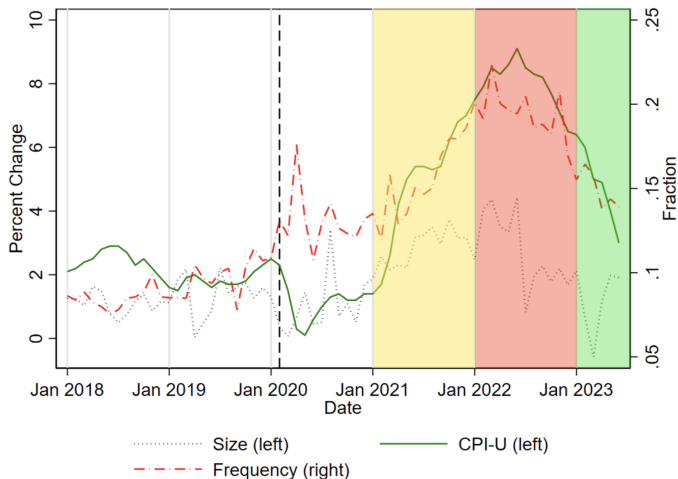
Figure 1: Montag and Villar, 2023



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Figure 1: Montag and Villar, 2023



- Great paper!
- Would like to see some more work on the quantitative side of the model
  - How important is it?
  - What's the most likely shape of the NL PC?
- Fantastic foundation for future work:
  1. Normative implications for a world with larger supply shocks
  2. Normative analysis with wage stickiness or multiple sectors
  3. Normative analysis for other types of lumpiness (labor, investment etc.)

**Thank you for your attention!**



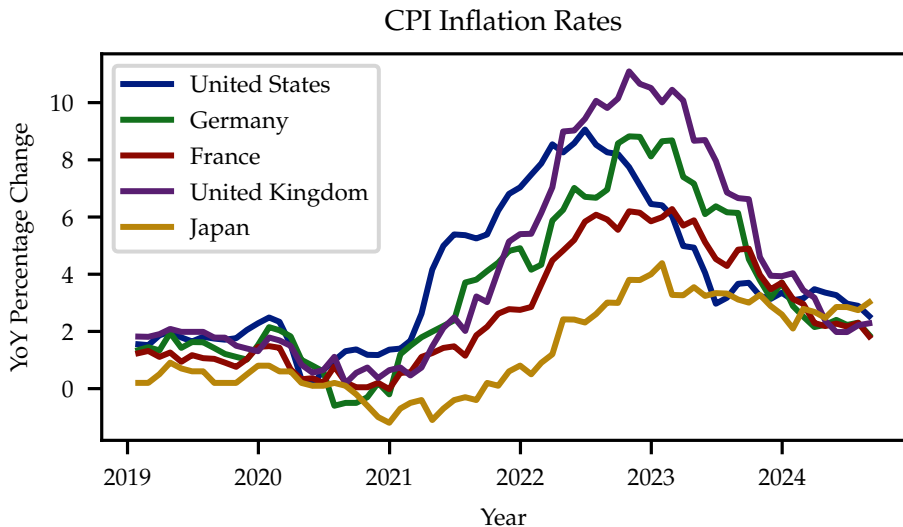
## Quote from Isabel Schnabel (22nd July 2024)

*We are no longer in a situation where inflation is persistently too low. On the contrary, many fear that we could face inflationary supply-side shocks more frequently in the future. We should look at how we can reliably fulfil our price stability mandate in such an environment.*

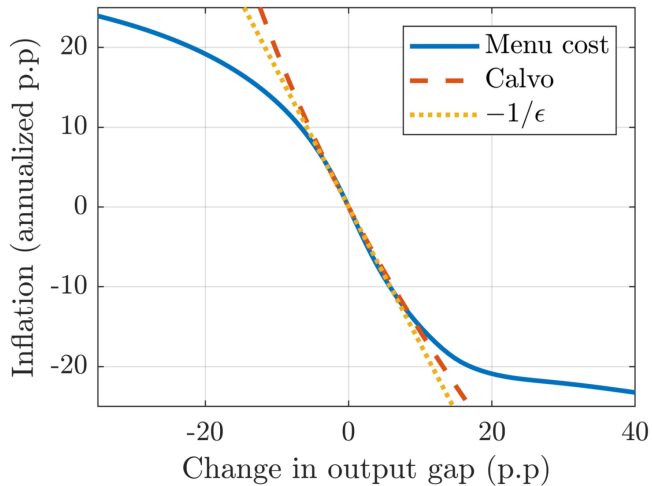
**Interview with Isabel Schnabel, Member of the Executive Board of the ECB, conducted by Christian Siedenbiedel (FAZ) on 22 July 2024**

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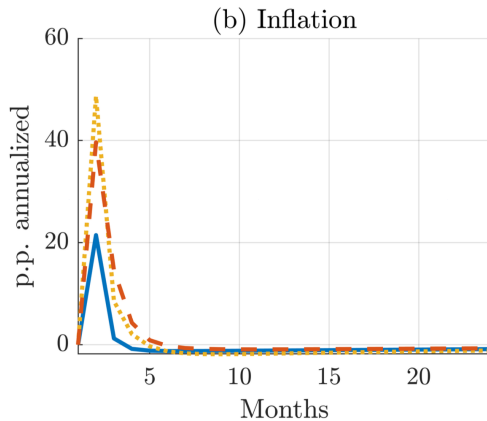
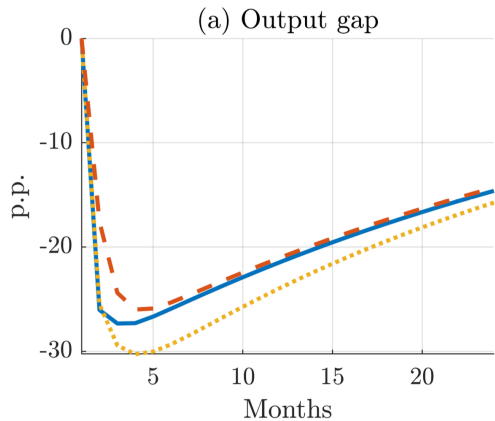
# Inflation between 2019 and 2024



# Optimal Targeting Rules



# Model IRFs



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